

2.4 Key features of graphs

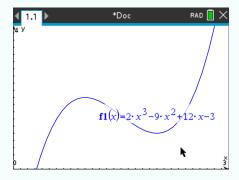
2.4.1 Find the maximum or minimum of a function, and its range

Find a local maximum or minimum

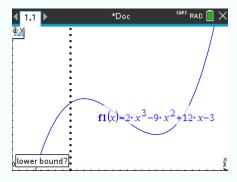
Suppose you want to know the local maximum(s) and minimum(s) of the following function:

$$f(x) = 2x^3 - 9x^2 + 12x - 3$$

① Enter the function and graph it properly. Here we choose **Xmin**= 0, **Xmax**= 3, **Ymin**= 0, **Ymax**= 4:



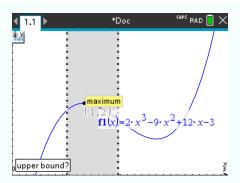
- 2 Press and select Analyze Graph > Maximum.
- 3 Choose a left bound (as asked at the bottom of the screen) until you reach the left of the local maximum:



Press enter

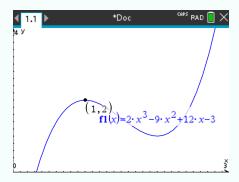
④ Choose a right bound (as asked at the bottom of the screen):





Press enter

5 Read the maximum:



Press enter

The result should be x = 1 and y = 2 (it is displayed next to the point).

You can apply the same procedure to find a local minimum by pressing select Analyze Graph > Minimum instead of select Analyze Graph > Maximum.

Find together the range, the global maximum and the global minimum of a function within a domain



This strategy is useful when one one only wants the y values of the global maximum or minimum. If you have to know the x values too, see 2.4.1

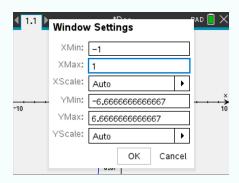
Suppose you want to find the maximum and minimum of the following function:

$$f(x) = x^3 - x + 1, \quad -1 \le x \le 1.$$

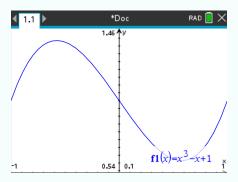
① Input the function



② Press and select Window / Zoom > Window Settings and fill **Xmin** and **Xmax** accordingly to the domain of the function:

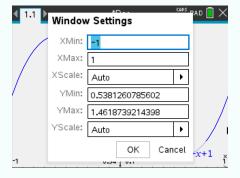


③ Press and select Window / Zoom > Zoom - Fit, and wait. The following should display:



Zoom-fit fits the y axis to match the range of f

Press and select Window / Zoom > Window Settings again, and read the values of Ymin and Ymax:



Thus, the minimum of f is 0.538, and the maximum is 1.462. Thus, the range of f is

$$0.538 \le y \le 1.462.$$



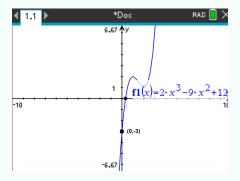
2.4.2 Find the y-intercept of a function

Suppose you want to know the y-intercept of the following function:

$$f(x) = 2x^3 - 9x^2 + 12x - 3$$

Recall that we want to compute f(0).

- ① Enter the function, and display its graph.
- ② Press and select Trace > Graph Trace. Press and it automatically shows the y-intercept.



The result **Y=-3** should be displayed within the coordinate of the point (at the bottom right of the screen).

2.4.3 Find one of the *x*-intercepts of a function

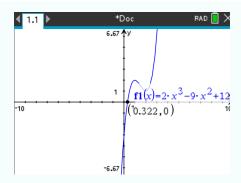
Suppose you want to know the x-intercept of the following function:

$$f(x) = 2x^3 - 9x^2 + 12x - 3$$

Recall that we want to compute the value of x when f(x) = 0.

- ① Enter the function, and display its graph.
- 2 Press and select Analyze Graph > Zero. Select lower and upper bounds the widest possible. Press enter.





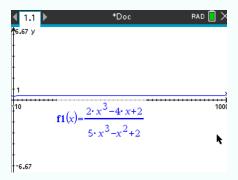
The result X=0.322 should be displayed within the coordinate of the point.

2.4.4 Find a horizontal asymptote of a function

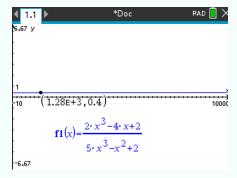
Suppose you want to see the horizontal asymptote of the following function when x goes to ∞ :

$$\frac{2x^3 - 4x + 2}{5x^3 - x^2 + 2}$$

① Enter the function and display huge values of x, like $\mathbf{Xmax} = 10000$:



② Press , select Analyze Graph > Maximum and take the y value of the maximum as the value of the horitzontal asymptote:



The result should be Y=0.4 (rounded).

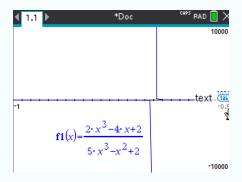


2.4.5 Find a vertical asymptote of a function

Suppose you want to see a vertical asymptote of the following function:

$$\frac{2x^3 - 4x + 2}{5x^3 - x^2 + 2}$$

① Enter the function and display x-values near the vertical asymptote and big y-values, here Xmin=-1, Xmax=-0.5, Ymin=-10000 and Ymax=10000:



- ② Use the maximum and minimum to find the x-value of each vertical asymptote. The x-values should be X=-0.678 at the left and X=-0.674 at the right (rounded).
- 3 Take the average of the two values.

The result should be x = 0.676 (rounded).



Depending on how precise you want the result to be, you will have to zoom in more, and move again the cursor

Here, by choosing **Xmin=-0.7** and **Xmax=-0.6** we get the result x = 0.67613 (rounded).

2.4.6 Find the intersection of two curves

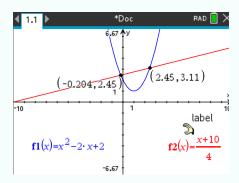
Suppose you want to know one of the intersections of the graphs of the following functions:

$$f(x) = x^2 - 2x + 2$$
 $g(x) = \frac{x+10}{4}$.

- ① Enter the two functions and graph them in order to see the intersection in question.
- ② Press and select Analyze Graph > Intersection.



- 3 Select right and left bound according to the intersection you want to know between the two intersections (right or left).
- ④ Press enter. The intersection point coordinates are displayed:



Press enter

The intersection points should be (-0.204,2.45) (left intersection point) and (2.45,3.11) (right intersection point) (rounded).