# 2.4 Key features of graphs

SCIEN

### 2.4.1 Find the maximum or minimum of a function, and its range

#### Find a local maximum or minimum

Suppose you want to know the local maximum(s) and minimum(s) of the following function:

$$f(x) = 2x^3 - 9x^2 + 12x - 3$$

① Enter the function and graph it properly. Here we choose Xmin= 0, Xmax= 3, Ymin= 0,
Ymax= 4:



- 2 Press and select Analyze Graph > Maximum.
- ③ Choose a left bound (as asked at the bottom of the screen) until you reach the left of the local maximum:



Press

④ Choose a right bound (as asked at the bottom of the screen):





The result should be x = 1 and y = 2 (it is displayed next to the point).

You can apply the same procedure to find a local minimum by pressing select Analyze Graph > Minimum instead of select Analyze Graph > Maximum.

# Find together the range, the global maximum and the global minimum of a function within a domain

This strategy is useful when one one only wants the y values of the global maximum or minimum. If you have to know the x values too, see 2.4.1

Suppose you want to find the maximum and minimum of the following function:

$$f(x) = x^3 - x + 1, \quad -1 \le x \le 1.$$

① Input the function



② Press and select Window / Zoom > Window Settings and fill Xmin and Xmax accordingly to the domain of the function:



③ Press and select Window / Zoom > Zoom - Fit, and wait. The following should display:



**Zoom-fit** fits the y axis to match the range of f

Press and select Window / Zoom > Window Settings again, and read the values of Ymin and Ymax:

<b>◀</b> 1.1 ▶	Window	/ Settings	CAPS	PAD 🗋 🗙
/	XMin:	-1		
	XMax:	1		
	XScale:	Auto	•	
/	YMin:	0.5381260785602		/
	YMax:	1.4618739214398		
	YScale:	Auto	•	1
		OK Car	ncel	-x+1 ×
-1		0.34 1 0.1		î

Thus, the minimum of f is 0.538, and the maximum is 1.462. Thus, the range of f is

 $0.538 \le y \le 1.462.$ 

#### 2.4.2 Find the y-intercept of a function

Suppose you want to know the y-intercept of the following function:

$$f(x) = 2x^3 - 9x^2 + 12x - 3$$

Recall that we want to compute f(0).

- ① Enter the function, and display its graph.
- 2 Press and select Trace > Graph Trace. Press and it automatically shows the y-intercept.



The result Y=-3 should be displayed within the coordinate of the point (at the bottom right of the screen).

#### 2.4.3 Find one of the x-intercepts of a function

Suppose you want to know the x-intercept of the following function:

$$f(x) = 2x^3 - 9x^2 + 12x - 3$$

Recall that we want to compute the value of x when f(x) = 0.

- ① Enter the function, and display its graph.
- 2 Press and select Analyze Graph > Zero. Select lower and upper bounds the widest possible. Press

TI-NSPIRE CX MANUAL FOR THE IB



The result X=0.322 should be displayed within the coordinate of the point.

## 2.4.4 Find a horizontal asymptote of a function

SCIENTIA

Suppose you want to see the horizontal asymptote of the following function when x goes to  $\infty$ :

$$\frac{2x^3 - 4x + 2}{5x^3 - x^2 + 2}$$

① Enter the function and display huge values of x, like **Xmax=10000**:



2 Press , select Analyze Graph > Maximum and take the y value of the maximum as the value of the horitzontal asymptote:



The result should be Y=0.4 (rounded).

#### 2.4.5 Find a vertical asymptote of a function

Suppose you want to see a vertical asymptote of the following function:

$$\frac{2x^3 - 4x + 2}{5x^3 - x^2 + 2}$$

① Enter the function and display x-values near the vertical asymptote and big y-values, here **Xmin=-1**, **Xmax=-0.5**, **Ymin=-10000** and **Ymax=10000**:



- <sup>(2)</sup> Use the maximum and minimum to find the x-value of each vertical asymptote. The x-values should be **X**=-0.678 at the left and **X**=-0.674 at the right (rounded).
- 3 Take the average of the two values.

The result should be x = 0.676 (rounded).

Depending on how precise you want the result to be, you will have to zoom in more, and move again the cursor

Here, by choosing **Xmin=-0.7** and **Xmax=-0.6** we get the result x = 0.67613 (rounded).

#### 2.4.6 Find the intersection of two curves

Suppose you want to know one of the intersections of the graphs of the following functions:

$$f(x) = x^2 - 2x + 2 \qquad \qquad g(x) = \frac{x + 10}{4}.$$

① Enter the two functions and graph them in order to see the intersection in question.

2 Press and select Analyze Graph > Intersection.



- ③ Select right and left bound according to the intersection you want to know between the two intersections (right or left).
- (4) Press enter . The intersection point coordinates are displayed:



```
Press enter
```

The intersection points should be (-0.204,2.45) (left intersection point) and (2.45,3.11) (right intersection point) (rounded).