

## 4.11 Statistical tests

### 4.11.1 $\chi^2$ test for independence

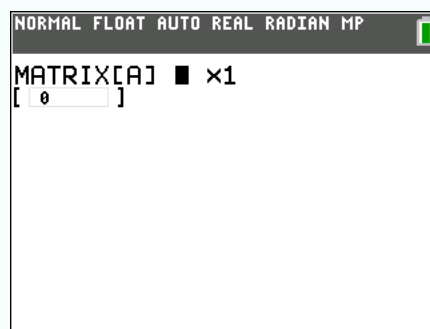
Consider the following set of data:

	Action	Horror	Comedy	Total
color-blind	120	90	40	250
non color-blind	110	95	45	250
Total	230	185	85	500

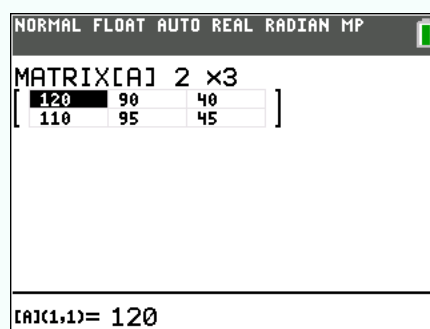
To be able to do a  $\chi^2$  test, you first need to put the data in a matrix.

#### Enter the data

① Press **2nd**, **matrix**, **EDIT**, **[A]**:



② Ignoring the “Total” rows and columns, set the matrix amount of rows and columns (here:  $2 \times 3$ ), and enter the data:

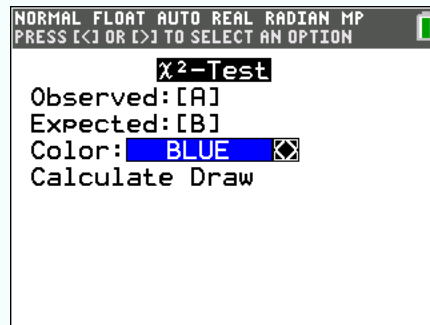


## Do the test

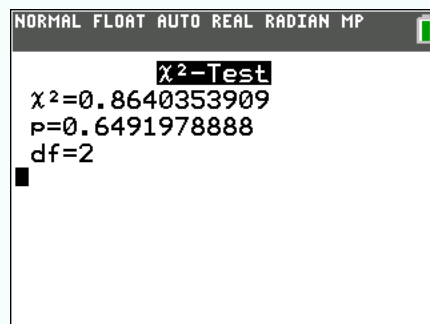
① Press  , TESTS,  $\chi^2$  -Test....

Set matrix [A] as **Observed** by pressing  ,  ,  .

Set a new matrix, e.g. matrix [B], as **Expected** by pressing  ,  ,  :



② Press **Calculate**. The following result should appear:



df means “degrees of freedom”

### 4.11.2 $\chi^2$ goodness of fit test

Consider a person counting the amount of cyclists he sees passing by his street each day:



Monday	Tuesday	Wednesday	Thursday	Friday	Saturday	Sunday
50	60	42	48	52	58	61

The null and alternative hypothesis are

$H_0$  : An equal amount of cyclists pass by his street each day.

$H_1$  : A different amount of cyclists pass by his street each day.

We want to know at a significance level of 0.05 if he must accept null hypothesis.


- ① Press  **stat**  **list** **Edit...** and enter the data in a list (here:  $L_1$ )
- ② fill  $L_2$  with the average amount of cyclists (here: 52.8).

Tip: you can highlight  $L_2$  and write  $\theta * L_1 + 52.8$  to fill it quickly.

NORMAL FLOAT AUTO a+bi RADIAN MP					
L1	L2	L3	L4	L5	L6
20	52.8	----	----	----	
60	52.8				
40	52.8				
48	52.8				
52	52.8				
58	52.8				
81	52.8				
----	----				

L2(8)=

- ③ Press  , TESTS,  $\chi^2$  GOF-Test and fill the parameters as follows:



NORMAL FLOAT AUTO  $\alpha$ +bi RADIAN MP  
 **$\chi^2$ GOF-Test**  
 Observed:L1  
 Expected:L2  
 df:6  
 Color: BLUE  
 Calculate Draw

$$\mathbf{df} = 7 - 1 \text{ (degrees of freedom),}$$

**Color** doesn't matter

Press Calculate

The results should be  $\chi^2 = 6.467$  (for the critical value) and  $p = 0.373$  (for the significance level), rounded.

We must then accept the null hypothesis.

### 4.11.3 The student's t-test

Consider the following data:

$\mathbf{x}_1$	2.8	3.2	2.7	3.5	3.0	2.9	4.1	3.9	
$\mathbf{x}_2$	3.1	3.5	2.8	3.7	4.2	2.6	3.2	2.9	3.8

You want to test whether the  $x_1$  data is on average a than  $x_2$  ( $\mu_1 > \mu_2$ ), at a significance level of 10%

- ① Press  , **Edit...** and enter both lists (here:  $x_1$  in  $L_1$  and  $x_2$  in  $L_2$ ):

L1	L2	L3	L4	L5	2
2.8	3.1	-----	-----	-----	
3.2	3.5				
2.7	2.8				
3.5	3.7				
3	4.2				
2.9	2.6				
4.1	3.2				
3.9	2.9				
-----	3.8				
	-----				
L2(10)=					

- ② Press  , **TESTs**, **2-SampTTest...** and enter the parameters as follow:

NORMAL	FLOAT	AUTO	a+bi	DEGREE	MP
2-SampTTest					
Inpt:	Data	Stats			
List1:	L1				
List2:	L2				
Freq1:	1				
Freq2:	1				
$\mu_1$ :	$\neq \mu_2$	$< \mu_2$	$> \mu_2$		
Pooled:	No	Yes			
Color:	BLUE				
Calculate	Draw				

Press ,  to get  $L_1$ ,

**Color** doesn't matter

Press **Calculate**.

The  $t$ -value should be  $t = -0.191$  and the  $p$ -value should be  $p = 0.575$  (rounded). Therefore we must accept the null hypothesis (we **cannot** infer that  $\mu_1 > \mu_2$ ).