# 4.11 Statistical tests

SCIENTIA

## 4.11.1 $\chi^2$ test for independence

Consider the following set of data:

	Action	Horror	Comedy	Total
color-blind	120	90	40	250
non color-blind	110	95	45	250
Total	230	185	85	500

To be able to do a  $\chi^2$  test, you first need to put the data in a matrix.

### Enter the data

A]:
NORMAL FLOAT AUTO REAL RADIAN MP MATRIX[A] ■ ×1 [ 0 ]

<sup>(2)</sup> Ignoring the "Total" rows and columns, set the matrix amount of rows and columns (here:  $2 \times 3$ ), and enter the data:

NORMAL FLOAT A	UTO REAL	RADIAN	MP [	]
MATRIX[A] 120 90 110 95	2 ×3 40 45	]		
[A](1,1)= 120				



#### Do the test

1	Press stat , TESTS, X <sup>2</sup> -Test
	Set matrix [A] as Observed by pressing $2nd$ , $\mathbf{x}^{1}$ , $1$ .
	Set a new matrix, e.g. matrix [B], as Expected by pressing $[2nd]$ , $[x^2]$ , $[2]$ :
	NORMAL FLOAT AUTO REAL RADIAN MP PRESS [<] OR [>] TO SELECT AN OPTION X2-Test Observed: [A] Expected: [B] Color: BLUE Calculate Draw

2 Press Calculate. The following result should appear:

<u>x2-Test</u>	
1 1 - 2 - 2 - 2 - 2 - 2 - 2 - 2 - 2 - 2	
P=0.6491978888 df=2	

df means "degrees of freedom"

# 4.11.2 $\chi^2$ goodness of fit test

Consider a person counting the amount of cyclists he sees passing by his street each day:

Monday	Tuesday	Wednesday	Thursday	Friday	Saturday	Sunday
50	60	42	48	52	58	61

The null and alternative hypthesis are

 $H_0$ : An equal amount of cyclists pass by his street each day.

 $H_1$ : A different amount of cyclists pass by his street each day.

We want to know at a significance level of 0.05 if he must accept null hypothesis.



- (1) Press state , Edit... and enter the data in a list (here:  $L_1$ )
- 2 fill  $L_2$  with the average amount of cyclists (here: 52.8).

Tip: you can highlight  $L_2$  and write  $0^*L_1+52.\,8$  to fill it quickly.

NORMAL	FLOAT AL	JTO a+bi	, RADIAN	MP			
L1	L2	Lз	L4	Ls	2		
20 60 40 52 58 81 	52.8 52.8 52.8 52.8 52.8 52.8 52.8 52.8						
L2(8)=							

(3) Press state , TESTS, X<sup>2</sup> GOF-Test and fill the parameters as follows:



df = 7 - 1 (degrees of freedom),

**Color** doesn't matter

#### $\operatorname{Press}$ Calculate

The results should be  $\chi^2 = 6.467$  (for the critical value) an p = 0.373 (for the epsignificance level), rounded.

We must then accept the null hypothesis.

### 4.11.3 The student's t-test

Consider the following data:

$x_1$	2.8	3.2	2.7	3.5	3.0	2.9	4.1	3.9	
$x_2$	3.1	3.5	2.8	3.7	4.2	2.6	3.2	2.9	3.8



You want to test whether the  $x_1$  data is on average a than  $x_2$  ( $\mu_1 > \mu_2$ ), at a significance level of 10%



NORMAL	FLOAT AL	JTO a+bi	, DEGREE	MP	Ō
L1	L2	Lз	L4	Ls	2
2.8 3.2 2.7 3.5 3 2.9 4.1 3.9	3.1 3.5 2.8 3.7 4.2 2.6 3.2 2.9 3.8				
L					

2 Press stat , TESTS, 2-SampTTest... and enter the parameters as follow:



### Press Calculate.

The *t*-value should be t = -0.191 and the *p*-value should be p = 0.575 (rounded). Therefore we must accept the null hypothesis (we **cannot** infer that  $\mu_1 > \mu_2$ ).